

JEE-MAIN EXAMINATION – JANUARY 2025

VnK Academy Thane
(HELD ON WEDNESDAY 29TH JANUARY 2025)

TIME : 9:00 AM TO 12:00 NOON

MATHEMATICS

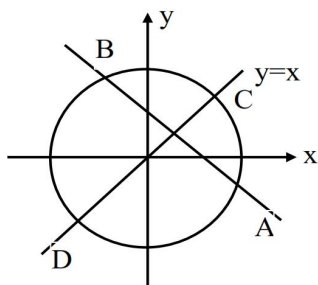
SECTION-A

1. Let the line $x + y = 1$ meet the circle $x^2 + y^2 = 4$ at the points A and B. If the line perpendicular to AB and passing through the mid point of the chord AB intersects the circle at C and D, then the area of the quadrilateral ADCB is equal to

- (1) $3\sqrt{7}$ (2) $2\sqrt{14}$
(3) $5\sqrt{7}$ (4) $\sqrt{14}$

Ans. (2)

Sol.



By solving $x = y$ with circle

We get

$$C(\sqrt{2}, \sqrt{2})$$

$$D(-\sqrt{2}, -\sqrt{2})$$

By solving $x + y = 1$ with

circle $x^2 + y^2 = 4$

we set

$$A\left(\frac{1+\sqrt{7}}{2}, \frac{1-\sqrt{7}}{2}\right)$$

$$\& B\left(\frac{1-\sqrt{7}}{2}, \frac{1+\sqrt{7}}{2}\right)$$

\therefore Area of Quadrilateral ACBD

$= 2 \times \text{Area of } \triangle BCD$

$$= 2 \times \frac{1}{2} \begin{vmatrix} \sqrt{2} & \sqrt{2} & 1 \\ \frac{1-\sqrt{7}}{2} & \frac{1+\sqrt{7}}{2} & 1 \\ -\sqrt{2} & -\sqrt{2} & 1 \end{vmatrix}$$

$$= 2\sqrt{14}$$

2. Let M and m respectively be the maximum and the minimum values of

$$f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4 \sin 4x \\ \sin^2 x & 1 + \cos^2 x & 4 \sin 4x \\ \sin^2 x & \cos^2 x & 1 + 4 \sin 4x \end{vmatrix}, x \in \mathbb{R}$$

Then $M^4 - m^4$ is equal to :

- (1) 1280 (2) 1295
(3) 1040 (4) 1215

Ans. (1)

Sol. $f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4 \sin 4x \\ \sin^2 x & 1 + \cos^2 x & 4 \sin 4x \\ \sin^2 x & \cos^2 x & 1 + 4 \sin 4x \end{vmatrix}, x \in \mathbb{R}$

$$R_2 \rightarrow R_2 - R_1 \& R_3 \rightarrow R_3 - R_1$$

$$f(x) = \begin{vmatrix} 1 + \sin^2 x & \cos^2 x & 4 \sin 4x \\ -1 & 1 & 0 \\ -1 & 0 & 1 \end{vmatrix}$$

Expand about R_1 , we get

$$f(x) = 2 + 4 \sin 4x$$

$$\therefore M = \text{max value of } f(x) = 6$$

$$m = \text{min value of } f(x) = -2$$

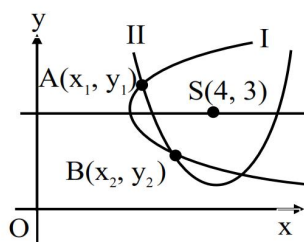
$$\therefore M^4 - m^4 = 1280$$

3. Two parabolas have the same focus (4,3) and their directrices are the x-axis and the y-axis, respectively. If these parabolas intersect at the points A and B, then $(AB)^2$ is equal to

- (1) 192 (2) 384
(3) 96 (4) 392

Ans. (1)

Sol.



Let intersection points of these two parabolas are

$A(x_1, y_1)$ & $B(x_2, y_2)$

\therefore equation of parabola I and II are given below

$$\therefore (x-4)^2 + (y-3)^2 = x^2 \quad \dots(1)$$

$$\& (x-4)^2 + (y-3)^2 = y^2 \quad \dots(2)$$

Here $A(x_1, y_1)$ & $B(x_2, y_2)$ will satisfy the equation

Also from equations (1) & (2), we get $x = y \dots(3)$

Put $x = y$ in equation (1)

$$\text{We get } x^2 - 14x + 25 = 0$$

$$x_1 + x_2 = 14$$

$$x_1 x_2 = 25$$

$$\therefore AB^2 = (x_1 - x_2)^2 + (y_1 - y_2)^2$$

$$= 2(x_1 - x_2)^2$$

$$= 2[(x_1 + x_2)^2 - 4x_1 x_2]$$

$$= 192$$

4. Let ABC be a triangle formed by the lines $7x - 6y + 3 = 0$, $x + 2y - 31 = 0$ and $9x - 2y - 19 = 0$, Let the point (h, k) be the image of the centroid of ΔABC in the line $3x + 6y - 53 = 0$. Then $h^2 + k^2 + hk$ is equal to

$$(1) 37$$

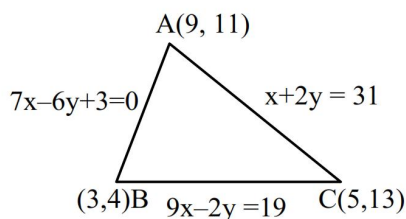
$$(2) 47$$

$$(3) 40$$

$$(4) 36$$

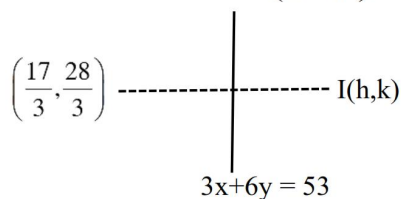
Ans. (1)

Sol.



$$\therefore \text{centroid of } \Delta ABC = \left(\frac{9+3+5}{3}, \frac{11+4+13}{3} \right)$$

$$= \left(\frac{17}{3}, \frac{28}{3} \right)$$



Let image of centroid with respect to line mirror is (h, k)

$$\therefore \left(\frac{k - \frac{28}{3}}{h - \frac{17}{3}} \right) \left(-\frac{1}{2} \right) = -1$$

$$\& 3 \left(\frac{h + \frac{17}{3}}{2} \right) + 6 \left(\frac{k + \frac{28}{3}}{2} \right) = 53$$

Solving (1) & (2) we get $h = 3$, $k = 4$

$$\therefore h^2 + k^2 + hk = 37$$

5. Let $\vec{a} = 2\hat{i} - \hat{j} + 3\hat{k}$, $\vec{b} = 3\hat{i} - 5\hat{j} + \hat{k}$ and \vec{c} be a vector such that $\vec{a} \times \vec{c} = \vec{c} \times \vec{b}$ and $(\vec{a} + \vec{c}) \cdot (\vec{b} + \vec{c}) = 168$. Then the maximum value

of $|\vec{c}|^2$ is :

$$(1) 77$$

$$(2) 462$$

$$(3) 308$$

$$(4) 154$$

Ans. (3)

$$\text{Sol. } \vec{a} = 2\hat{i} - \hat{j} + 3\hat{k}$$

$$\vec{b} = 3\hat{i} - 5\hat{j} + \hat{k}$$

$$\vec{a} \times \vec{c} = \vec{c} \times \vec{b}$$

$$\vec{a} \times \vec{c} + \vec{b} \times \vec{c} = 0$$

$$(\vec{a} + \vec{b}) \times \vec{c} = 0$$

$$\Rightarrow \vec{c} = \lambda(\vec{a} + \vec{b})$$

$$\vec{c} = \lambda(5\hat{i} - 6\hat{j} + 4\hat{k}) \dots(1)$$

$$|\vec{c}|^2 = \lambda^2(25 + 36 + 16)$$

$$|\vec{c}|^2 = 77\lambda^2$$

$$(\vec{a} + \vec{c}) \cdot (\vec{b} + \vec{c}) = 168$$

$$\vec{a} \cdot \vec{b} + \vec{a} \cdot \vec{c} + \vec{c} \cdot \vec{b} + |\vec{c}|^2 = 168$$

$$14 + \vec{c} \cdot (\vec{a} + \vec{b}) + 77\lambda^2 = 168$$

using equation (1)

$$\lambda[5\hat{i} - 6\hat{j} + 4\hat{k}]^2 + 77\lambda^2 = 154$$

$$77\lambda + 77\lambda^2 - 154 = 0$$

$$\lambda^2 + \lambda - 2 = 0$$

$$\lambda = -2, 1$$

\therefore Maximum value of $|\vec{c}|^2$ occurs when $\lambda = -2$

$$|\vec{c}|^2 = 77\lambda^2$$

$$= 77 \times 4$$

$$= 308$$

6. Let P be the set of seven digit numbers with sum of their digits equal to 11. If the numbers in P are formed by using the digits 1, 2 and 3 only, then the number of elements in the set P is :

- (1) 158 (2) 173
(3) 164 (4) 161

Ans. (4)

Sol. (i) number of numbers created using

$$1111133 = \frac{7!}{5!2!} \Rightarrow 21$$

(ii) number of numbers created using

$$1111223 = \frac{7!}{4!2!} \Rightarrow 105$$

(iii) number of numbers created using

$$1112222 = \frac{7!}{4!3!} \Rightarrow 35$$

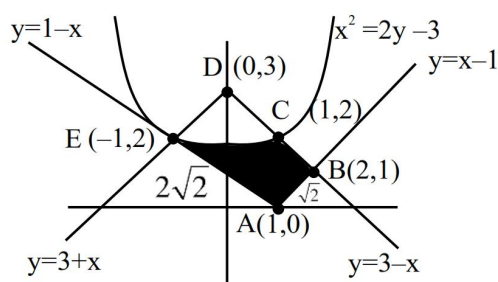
$$\text{Total} = 161$$

7. Let the area of the region $\{(x, y) : 2y \leq x^2 + 3, y + |x| \leq 3, y \geq |x - 1|\}$ be A. Then 6A is equal to:

- (1) 16 (2) 12
(3) 18 (4) 14

Ans. (4)

Sol.



A \Rightarrow Rectangle ABDE - Area of region EDC

$$A \Rightarrow 4 - 2 \int_0^1 (3 - x) - \left(\frac{x^2 + 3}{2} \right) dx$$

$$A \Rightarrow 4 - 2 \left\{ 3x - \frac{x^2}{2} - \frac{x^3}{6} - \frac{3}{2}x \right\}_0^1$$

$$A \Rightarrow 4 - 2 \left\{ 3 - \frac{1}{2} - \frac{1}{6} - \frac{3}{2} \right\} = \frac{7}{3}$$

$$\text{So } 6A = 14$$

8. The least value of n for which the number of integral terms in the Binomial expansion of

$$\left(\sqrt[3]{7} + \sqrt[12]{11} \right)^n \text{ is } 183, \text{ is :}$$

- (1) 2184 (2) 2148
(3) 2172 (4) 2196

Ans. (1)

Sol. General term = ${}^nC_r \left(7^{1/3} \right)^{n-r} \left(11^{1/12} \right)^r$

$$= {}^nC_r \left(7 \right)^{\frac{n-r}{3}} \left(11 \right)^{r/12}$$

For integral terms, r must be multiple of 12

$$\therefore r = 12k, k \in W$$

Total values of r = 183

Hence max r = 12(182)

$$= 2184$$

Min value of n = 2184

9. The number of solutions of the equation

$$\left(\frac{9}{x} - \frac{9}{\sqrt{x}} + 2 \right) \left(\frac{2}{x} - \frac{7}{\sqrt{x}} + 3 \right) = 0 \text{ is :}$$

- (1) 2 (2) 4
(3) 1 (4) 3

Ans. (2)

Sol. Consider $\frac{1}{\sqrt{x}} = \alpha$ $x > 0$

$$(9\alpha^2 - 9\alpha + 2)(2\alpha^2 - 7\alpha + 3) = 0$$

$$(3\alpha - 2)(3\alpha - 1)(\alpha - 3)(2\alpha - 1) = 0$$

$$\alpha = \frac{1}{3}, \frac{1}{2}, \frac{2}{3}, 3$$

$$x = 9, 4, \frac{9}{4}, \frac{1}{9}$$

So, no. of solutions = 4

10. Let $y = y(x)$ be the solution of the differential equation

$$\cos x (\log_e (\cos x))^2 dy + (\sin x - 3y \sin x \log_e (\cos x)) dx = 0,$$

$x \in \left(0, \frac{\pi}{2}\right)$. If $y\left(\frac{\pi}{4}\right) = \frac{-1}{\log_e 2}$, then $y\left(\frac{\pi}{6}\right)$ is :

- (1) $\frac{2}{\log_e (3) - \log_e (4)}$ (2) $\frac{1}{\log_e (4) - \log_e (3)}$
 (3) $-\frac{1}{\log_e (4)}$ (4) $\frac{1}{\log_e (3) - \log_e (4)}$

Ans. (4)

Sol. $\cos x (\ln (\cos x))^2 dy + (\sin x - 3y (\sin x) \ln (\cos x)) dx = 0$

$$\cos x (\ln (\cos x))^2 \frac{dy}{dx} - 3 \sin x \cdot \ln (\cos x) y = -\sin x$$

$$\frac{dy}{dx} - \frac{3 \tan x}{\ln (\cos x)} y = \frac{-\tan x}{(\ln (\cos x))^2}$$

$$\frac{dy}{dx} + \frac{3 \tan x}{\ln (\sec x)} y = \frac{-\tan x}{(\ln (\sec x))^2}$$

$$\text{I.F.} = e^{\int \frac{3 \tan x}{\ln (\sec x)} dx} = (\ln (\sec x))^3$$

$$y \times (\ln (\sec x))^3 = -\int \frac{\tan x}{(\ln (\sec x))^2} (\ln (\sec x))^3 dx$$

$$y \times (\ln (\sec x))^3 = -\frac{1}{2} (\ln (\sec x))^2 + C$$

$$\text{Given : } x = \frac{\pi}{4}, y = -\frac{1}{\ln 2}$$

$$\frac{-1}{\ln 2} \times (\ln \sqrt{2})^3 = -\frac{1}{2} \times (\ln \sqrt{2})^2 + C$$

$$\Rightarrow \frac{-1}{8 \ln 2} \times (\ln 2)^3 = \frac{-1}{2} \times \frac{1}{4} (\ln 2)^2 + C$$

$$-\frac{1}{8} (\ln 2)^2 = \frac{-1}{8} (\ln 2)^2 + C$$

$$\Rightarrow C = 0$$

$$\therefore y (\ln (\sec x))^3 = \frac{-1}{2} (\ln (\sec x))^2 + 0$$

$$y = \frac{-1}{2 \ln (\sec x)}$$

$$y = \frac{1}{2 \ln (\cos x)}$$

$$\therefore y\left(\frac{\pi}{6}\right) = \frac{1}{2 \ln \left(\cos \frac{\pi}{6}\right)}$$

$$= \frac{1}{2 \ln \left(\frac{\sqrt{3}}{2}\right)}$$

$$= \frac{1}{2 \left(\frac{1}{2} \ln 3 - \ln 2\right)}$$

$$= \frac{1}{\ln 3 - \ln 4}$$

Option (4)

11. Define a relation R on the interval $\left[0, \frac{\pi}{2}\right]$ by $x R y$

if and only if $\sec^2 x - \tan^2 y = 1$. Then R is :

- (1) an equivalence relation
 (2) both reflexive and transitive but not symmetric
 (3) both reflexive and symmetric but not transitive
 (4) reflexive but neither symmetric nor transitive

Ans. (1)

Sol. $\sec^2 x - \tan^2 x = 1$ (on replacing y with x)

\Rightarrow Reflexive

$$\sec^2 x - \tan^2 y = 1$$

$$\Rightarrow 1 + \tan^2 x + 1 - \sec^2 y = 1$$

$$\Rightarrow \sec^2 y - \tan^2 x = 1$$

\Rightarrow symmetric

$$\sec^2 x - \tan^2 y = 1,$$

$$\sec^2 y - \tan^2 z = 1$$

Adding both

$$\Rightarrow \sec^2 x - \tan^2 y + \sec^2 y - \tan^2 z = 1 + 1$$

$$\sec^2 x + 1 - \tan^2 z = 2$$

$$\sec^2 x - \tan^2 z = 1$$

\Rightarrow Transitive

hence equivalence relation

Option (1)

12. Let the ellipse, $E_1 : \frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, $a > b$ and

$$E_2 : \frac{x^2}{A^2} + \frac{y^2}{B^2} = 1, A < B \text{ have same eccentricity}$$

$$\frac{1}{\sqrt{3}}. \text{ Let the product of their lengths of latus}$$

$$\text{rectums be } \frac{32}{\sqrt{3}}, \text{ and the distance between the foci}$$

of E_1 be 4. If E_1 and E_2 meet at A,B,C and D, then the area of the quadrilateral ABCD equals:

$$(1) 6\sqrt{6} \quad (2) \frac{18\sqrt{6}}{5}$$

$$(3) \frac{12\sqrt{6}}{5} \quad (4) \frac{24\sqrt{6}}{5}$$

Ans. (4)

Sol. $2ae = 4$

$$2a\left(\frac{1}{\sqrt{3}}\right) = 4$$

$$\Rightarrow a = 2\sqrt{3}$$

$$\Rightarrow 1 - \frac{b^2}{12} = \frac{1}{3} \Rightarrow b^2 = 8$$

$$\text{Now } \frac{2b^2}{a} \cdot \frac{2A^2}{B} = \frac{32}{\sqrt{3}} \Rightarrow 2\left(\frac{8}{2\sqrt{3}}\right) \frac{2A^2}{B} = \frac{32}{\sqrt{3}}$$

$$\Rightarrow A^2 = 2B$$

$$1 - \frac{A^2}{B^2} = \frac{1}{3} \Rightarrow 1 - \frac{2B}{B^2} = \frac{1}{3} \Rightarrow B = 3$$

$$\Rightarrow A^2 = 6$$

$$\frac{x^2}{12} + \frac{y^2}{8} = 1 \dots\dots(1)$$

$$\frac{x^2}{6} + \frac{y^2}{9} = 1 \dots\dots(2)$$

On solving (1) & (2) we get

$$(x, y) \equiv \left(\frac{\sqrt{6}}{\sqrt{5}}, \frac{6}{\sqrt{5}}\right), \left(\frac{-\sqrt{6}}{\sqrt{5}}, \frac{6}{\sqrt{5}}\right), \left(\frac{\sqrt{6}}{\sqrt{5}}, \frac{-6}{\sqrt{5}}\right), \left(\frac{-\sqrt{6}}{\sqrt{5}}, \frac{-6}{\sqrt{5}}\right)$$

The four points are vertices of rectangle and its area =

$$\frac{24\sqrt{6}}{5}$$

13. Consider an A.P. of positive integers, whose sum of the first three terms is 54 and the sum of the first twenty terms lies between 1600 and 1800. Then its 11th term is :

- (1) 84 (2) 122
(3) 90 (4) 108

Ans. (3)

Sol. $S_3 = 3a + 3d = 54$

$$\Rightarrow a + d = 18$$

$$S_{20} = 10(2a + 19d)$$

$$\Rightarrow 10(36 + 17d)$$

$$\Rightarrow 1600 < 10(36 + 17d) < 1800$$

$$\Rightarrow 160 < 36 + 17d < 180$$

$$\Rightarrow 124 < 17d < 144$$

$$\Rightarrow 7\frac{5}{17} < d < 8\frac{8}{17}$$

Common difference will be natural number

$$\Rightarrow d = 8 \Rightarrow a = 10$$

$$\Rightarrow a_{11} = 10 + 10 \times 8 = 90$$

14. Let $\vec{a} = \hat{i} + 2\hat{j} + \hat{k}$ and $\vec{b} = 2\hat{i} + 7\hat{j} + 3\hat{k}$. Let

$$L_1 : \vec{r} = (-\hat{i} + 2\hat{j} + \hat{k}) + \lambda \vec{a}, \lambda \in \mathbb{R} \text{ and}$$

$$L_2 : \vec{r} = (\hat{j} + \hat{k}) + \mu \vec{b}, \mu \in \mathbb{R} \text{ be two lines. If the}$$

line L_3 passes through the point of intersection of L_1 and L_2 , and is parallel to $\vec{a} + \vec{b}$, then L_3 passes through the point:

- (1) (8, 26, 12) (2) (2, 8, 5)
(3) (-1, -1, 1) (4) (5, 17, 4)

Ans. (1)

Sol. $L_1 : \vec{r} = (-\hat{i} + 2\hat{j} + \hat{k}) + \lambda(\hat{i} + 2\hat{j} + \hat{k})$

$$\Rightarrow \vec{r} = (\lambda - 1)\hat{i} + 2(\lambda + 1)\hat{j} + (\lambda + 1)\hat{k}$$

$$L_2 : \vec{r} = (\hat{j} + \hat{k}) + \mu(2\hat{i} + 7\hat{j} + 3\hat{k})$$

$$\Rightarrow \vec{r} = 2\mu\hat{i} + (1 + 7\mu)\hat{j} + (1 + 3\mu)\hat{k}$$

For point of intersection equating respective components

$$\Rightarrow \lambda - 1 = 2\mu \dots(1)$$

$$2(\lambda + 1) = 1 + 7\mu \dots(2)$$

$$\lambda + 1 = 1 + 3\mu \dots(3)$$

We get

$$\Rightarrow \lambda = 3 \text{ and } \mu = 1$$

$$\Rightarrow \vec{a} + \vec{b} = 3\hat{i} + 9\hat{j} + 4\hat{k}$$

$$L_3 : \vec{r} = 2\hat{i} + 8\hat{j} + 4\hat{k} + \alpha(3\hat{i} + 9\hat{j} + 4\hat{k})$$

$$\text{For } \alpha = 2, \vec{r} = 8\hat{i} + 26\hat{j} + 12\hat{k}$$

15. The value of $\lim_{n \rightarrow \infty} \left(\sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 5}{(k+3)!} \right)$ is :

(1) $\frac{4}{3}$ (2) 2

(3) $\frac{7}{3}$ (4) $\frac{5}{3}$

Ans. (4)

Sol. $\lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 5}{(k+3)!}$

$$= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{k^3 + 6k^2 + 11k + 6 - 1}{(k+3)!}$$

$$= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{(k+1)(k+2)(k+3) - 1}{(k+3)!}$$

$$= \lim_{n \rightarrow \infty} \sum_{k=1}^n \frac{(k+1)(k+2)(k+3)}{(k+3)!} - \frac{1}{(k+3)!}$$

$$= \lim_{n \rightarrow \infty} \sum_{k=1}^n \left(\frac{1}{k!} - \frac{1}{(k+3)!} \right)$$

$$= \lim_{n \rightarrow \infty} \left(\frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} \dots + \frac{1}{n!} - \frac{1}{4!} - \frac{1}{5!} - \frac{1}{6!} \dots - \frac{1}{(n+3)!} \right)$$

$$= \frac{1}{1} + \frac{1}{2} + \frac{1}{6} = \frac{10}{6} = \frac{5}{3}$$

16. The integral $80 \int_0^{\frac{\pi}{4}} \left(\frac{\sin \theta + \cos \theta}{9 + 16 \sin 2\theta} \right) d\theta$ is equal to :

(1) $3 \log_e 4$ (2) $6 \log_e 4$

(3) $4 \log_e 3$ (4) $2 \log_e 3$

Ans. (3)

Sol. $I = 80 \int_0^{\frac{\pi}{4}} \left(\frac{\sin \theta + \cos \theta}{9 + 16(2 \sin \theta \cos \theta)} \right) d\theta$

$$= 80 \int_0^{\frac{\pi}{4}} \frac{\sin \theta + \cos \theta}{9 - 16(1 - 2 \sin \theta \cos \theta - 1)} d\theta$$

$$= 80 \int_0^{\frac{\pi}{4}} \frac{\sin \theta + \cos \theta}{9 + 16 - 16(\sin \theta - \cos \theta)^2} d\theta$$

Let $\sin \theta - \cos \theta = t$

$(\cos \theta + \sin \theta) d\theta = dt$

$$= 80 \int_{-1}^0 \frac{dt}{25 - 16t^2}$$

$$= \frac{80}{16} \int_{-1}^0 \frac{dt}{\left(\frac{5}{4}\right)^2 - t^2}$$

$$= \frac{5}{2 \left(\frac{5}{4}\right)} \ln \left| \frac{\frac{5}{4} + t}{\frac{5}{4} - t} \right| \Bigg|_{-1}^0$$

$$= 2 \ln(1) + 4 \ln 3$$

$$= 4 \ln 3$$

17. Let $L_1 : \frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{2}$ and

$L_2 : \frac{x+1}{-1} = \frac{y-2}{2} = \frac{z}{1}$ be two lines.

Let L_3 be a line passing through the point (α, β, γ) and be perpendicular to both L_1 and L_2 . If L_3 intersects L_1 , then $|5\alpha - 11\beta - 8\gamma|$ equals :

(1) 18 (2) 16
(3) 25 (4) 20

Ans. (3)

Sol. DR's of $L_3 = \vec{m} \times \vec{n} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & -1 & 2 \\ -1 & 2 & 1 \end{vmatrix}$

$$= -5\hat{i} - 3\hat{j} + \hat{k}$$

$$L_3 : \frac{x-\alpha}{-5} = \frac{y-\beta}{-3} = \frac{z-\gamma}{1} = \lambda$$

$$A(\alpha - 5\lambda, \beta - 3\lambda, \gamma + \lambda)$$

$$L_1 : \frac{x-1}{1} = \frac{y-2}{-1} = \frac{z-1}{2} = k$$

$$B(k+1, -k+2, 2k+1)$$

Now

$$\alpha - 5\lambda = k+1 \Rightarrow \alpha = 5\lambda + k+1$$

$$\beta - 3\lambda = -k+2 \Rightarrow \beta = 3\lambda - k+2$$

$$\gamma + \lambda = 2k+1 \Rightarrow \gamma = -\lambda + 2k+1$$

$$|5\alpha - 11\beta - 8\gamma| = |-25|$$

$$= 25$$

18. Let x_1, x_2, \dots, x_{10} be ten observations such that

$$\sum_{i=1}^{10} (x_i - 2) = 30, \quad \sum_{i=1}^{10} (x_i - \beta)^2 = 98, \quad \beta > 2 \text{ and}$$

their variance is $\frac{4}{5}$. If μ and σ^2 are respectively the

mean and the variance of $2(x_1 - 1) + 4\beta, 2(x_2 - 1) +$

$4\beta, \dots, 2(x_{10} - 1) + 4\beta$, then $\frac{\beta\mu}{\sigma^2}$ is equal to :

- (1) 100 (2) 110
(3) 120 (4) 90

Ans. (1)

Sol. $\sum_{i=1}^{10} x_i = 50, \therefore \text{mean} = 5$

$$\text{Variance} = \frac{4}{5} = \frac{\sum x_i^2}{10} - \left(\frac{\sum x_i}{10} \right)^2$$

$$\frac{4}{5} = \frac{\sum x_i^2}{10} - 25$$

$$\Rightarrow \sum x_i^2 = 258 \quad \dots(1)$$

$$\text{Now } \sum_{i=1}^{10} (x_i - \beta)^2 = 98$$

$$\sum_{i=1}^{10} (x_i^2 - 2\beta x_i + \beta^2) = 98$$

$$258 - 2\beta(50) + 10\beta^2 = 98$$

$$(\beta - 8)(\beta - 2) = 0$$

$$\beta = 8 \text{ or } \beta = 2 \quad (\text{as } \beta > 2)$$

$$\therefore \beta = 8 \quad \dots(2)$$

Now as per the question

$$2(x_1 - 1) + 4\beta, 2(x_2 - 1) + 4\beta, \dots, 2(x_{10} - 1) + 4\beta$$

can be simplified to

$$2x_1 + 30, 2x_2 + 30, \dots, 2x_{10} + 30 \quad \text{using eq. (2)}$$

$$\mu = 2(5) + 30 = 40 \quad \dots(3)$$

$$\sigma^2 = 2^2 \left(\frac{4}{5} \right) = \frac{16}{5}$$

$$\therefore \frac{\beta\mu}{\sigma^2} = \frac{8 \times 40}{16/5} = 100$$

19. Let $|z_1 - 8 - 2i| \leq 1$ and $|z_2 - 2 + 6i| \leq 2$,

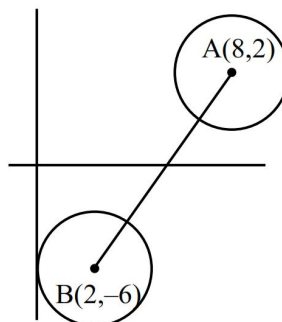
$z_1, z_2 \in \mathbb{C}$. Then the minimum value of $|z_1 - z_2|$

is :

- (1) 3 (2) 7
(3) 13 (4) 10

Ans. (2)

Sol.



$$\therefore AB = \sqrt{100} = 10$$

$$\therefore |Z_1 - Z_2|_{\min} = 10 - 2 - 1 = 7$$

20. Let $A = [a_{ij}] = \begin{bmatrix} \log_5 128 & \log_4 5 \\ \log_5 8 & \log_4 25 \end{bmatrix}$.

If A_{ij} is the cofactor of a_{ij} , $C_{ij} = \sum_{k=1}^2 a_{ik} A_{jk}$, $1 \leq i,$

$j \leq 2$, and $C = [C_{ij}]$, then $8|C|$ is equal to :

- (1) 262 (2) 288
(3) 242 (4) 222

Ans. (3)

$$|A| = \frac{11}{2}$$

$$C_{11} = \sum_{k=1}^2 a_{1k} \cdot A_{1k} = a_{11}A_{11} + a_{12}A_{12} = |A| = \frac{11}{2}$$

$$C_{12} = \sum_{k=1}^2 a_{1k} \cdot A_{2k} = 0$$

$$C_{21} = \sum_{k=1}^2 a_{2k} \cdot A_{1k} = 0$$

$$C_{22} = \sum_{k=1}^2 a_{2k} \cdot A_{2k} = |A| = \frac{11}{2}$$

$$C = \begin{bmatrix} 11/2 & 0 \\ 0 & 11/2 \end{bmatrix}$$

$$|C| = \frac{121}{4}$$

$$8|C| = 242$$

SECTION-B

21. Let $f : (0, \infty) \rightarrow \mathbb{R}$ be a twice differentiable

function. If for some $a \neq 0$, $\int_0^1 f(\lambda x) d\lambda = af(x)$,

$f(1) = 1$ and $f(16) = \frac{1}{8}$, then $16-f'\left(\frac{1}{16}\right)$ is equal

to _____,

Ans. (112)

Sol. $\int_0^1 f(\lambda x) d\lambda = af(x)$

$$\lambda x = t$$

$$d\lambda = \frac{1}{x} dt$$

$$\frac{1}{x} \int_0^x f(t) dt = af(x)$$

$$\int_0^x f(t) dt = axf(x)$$

$$f(x) = a(x f'(x) + f(x))$$

$$(1-a)f(x) = a.x f'(x)$$

$$\frac{f'(x)}{f(x)} = \frac{(1-a)}{a} \frac{1}{x}$$

$$\ln f(x) = \frac{1-a}{a} \ln x + c$$

$$x=1, f(1)=1 \Rightarrow c=0$$

$$x=16, f(16) = \frac{1}{8}$$

$$\frac{1}{8} = (16)^{\frac{1-a}{a}} \Rightarrow -3 = \frac{4-4a}{a} \Rightarrow a=4$$

$$f(x) = x^{-\frac{3}{4}}$$

$$f'(x) = -\frac{3}{4} x^{-\frac{7}{4}}$$

$$\therefore 16 - f'\left(\frac{1}{16}\right)$$

$$= 16 - \left(-\frac{3}{4}(2^{-4})^{-7/4}\right)$$

$$= 16 + 96 = 112$$

22. Let $S = \{m \in \mathbb{Z} : A^{m^2} + A^m = 3I - A^{-6}\}$, where

$$A = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}. \text{ Then } n(S) \text{ is equal to } \underline{\hspace{2cm}}.$$

Ans. (2)

$$\text{Sol. } A = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}$$

$$A^2 = \begin{bmatrix} 3 & -2 \\ 2 & -1 \end{bmatrix}, A^3 = \begin{bmatrix} 4 & -3 \\ 3 & -2 \end{bmatrix}, A^4 = \begin{bmatrix} 5 & -4 \\ 4 & -3 \end{bmatrix}$$

and so on

$$A^6 = \begin{bmatrix} 7 & -6 \\ 6 & -5 \end{bmatrix}$$

$$A^m = \begin{bmatrix} m+1 & -m \\ m & -m+1 \end{bmatrix},$$

$$A^{m^2} = \begin{bmatrix} m^2+1 & -m^2 \\ m^2 & -(m^2-1) \end{bmatrix}$$

$$A^{m^2} + A^m = 3I - A^{-6}$$

$$\begin{bmatrix} m^2+1 & -m^2 \\ m^2 & -(m^2-1) \end{bmatrix} + \begin{bmatrix} m+1 & -m \\ m & -m+1 \end{bmatrix}$$

$$= 3 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} - \begin{bmatrix} -5 & 6 \\ -6 & 7 \end{bmatrix}$$

$$= \begin{bmatrix} 8 & -6 \\ 6 & -4 \end{bmatrix}$$

$$= m^2 + 1 + m + 1 = 8$$

$$= m^2 + m - 6 = 0 \Rightarrow m = -3, 2$$

$$n(S) = 2$$

23. Let $[t]$ be the greatest integer less than or equal to t .

Then the least value of $p \in \mathbb{N}$ for which

$$\lim_{x \rightarrow 0^+} \left(x \left(\left[\frac{1}{x} \right] + \left[\frac{2}{x} \right] + \dots + \left[\frac{p}{x} \right] \right) - x^2 \left(\left[\frac{1}{x^2} \right] + \left[\frac{2^2}{x^2} \right] + \dots + \left[\frac{9^2}{x^2} \right] \right) \right) \geq 1$$

is equal to _____.

Ans. (24)

$$\text{Sol. } \lim_{x \rightarrow 0^+} \left(x \left(\left[\frac{1}{x} \right] + \left[\frac{2}{x} \right] + \dots + \left[\frac{p}{x} \right] \right) - x^2 \left(\left[\frac{1}{x^2} \right] + \left[\frac{2^2}{x^2} \right] + \left[\frac{9^2}{x^2} \right] \right) \right) \geq 1$$

$$(1 + 2 + \dots + p) - (1^2 + 2^2 + \dots + 9^2) \geq 1$$

$$\frac{p(p+1)}{2} - \frac{9 \cdot 10 \cdot 19}{6} \geq 1$$

$$p(p+1) \geq 572$$

Least natural value of p is 24

- 24.** The number of 6-letter words, with or without meaning, that can be formed using the letters of the word MATHS such that any letter that appears in the word must appear at least twice, is 4 ____.

Ans. (1405)

- Sol.** (i) Single letter is used, then no. of words = 5
(ii) Two distinct letters are used, then no. of words

$${}^5C_2 \times \left(\frac{6!}{2!4!} \times 2 + \frac{6!}{3!3!} \right) = 10(30 + 20) = 500$$

- (iii) Three distinct letters are used, then no. of words

$${}^5C_3 \times \frac{6!}{2!2!2!} = 900$$

Total no. of words = 1405

- 25.** Let $S = \{x : \cos^{-1} x = \pi + \sin^{-1} x + \sin^{-1} (2x+1)\}$.

Then $\sum_{x \in S} (2x-1)^2$ is equal to ____.

Ans. (5)

Sol. $\cos^{-1} x = \pi + \sin^{-1} x + \sin^{-1} (2x+1)$

$$2\cos^{-1} x - \sin^{-1} (2x+1) = \frac{3\pi}{2}$$

$$2\alpha - \beta = \frac{3\pi}{2} \text{ where } \cos^{-1} x = \alpha, \sin^{-1} (2x+1) = \beta$$

$$2\alpha = \frac{3\pi}{2} + \beta$$

$$\cos 2\alpha = \sin \beta$$

$$2\cos^2 \alpha - 1 = \sin \beta$$

$$2x^2 - 1 = 2x + 1$$

$$x^2 - x - 1 = 0$$

$$\Rightarrow x = \frac{1-\sqrt{5}}{2}, \left\{ x = \frac{1+\sqrt{5}}{2} \text{ rejected} \right\}$$

$$\therefore 4x^2 - 4x = 4$$

$$(2x-1)^2 = 5$$

PHYSICS

SECTION-A

26. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

Assertion (A) : Choke coil is simply a coil having a large inductance but a small resistance. Choke coils are used with fluorescent mercury-tube fittings. If household electric power is directly connected to a mercury tube, the tube will be damaged.

Reason (R) : By using the choke coil, the voltage across the tube is reduced by a factor $\left(\frac{R}{\sqrt{R^2 + \omega^2 L^2}}\right)$, where ω is frequency of the supply across resistor R and inductor L. If the choke coil were not used, the voltage across the resistor would be the same as the applied voltage. In the light of the above statements, choose the **most appropriate answer** from the options given below:

- (1) Both (A) and (R) are true but (R) is **not** the correct explanation of (A).
- (2) (A) is false but (R) is true.
- (3) Both (A) and (R) are true and (R) is the correct explanation of (A).
- (4) (A) is true but (R) is false.

Ans. (3)

Sol. A: Correct

B : Correct with correct explanation

27. Two projectiles are fired with same initial speed from same point on ground at angles of $(45^\circ - \alpha)$ and $(45^\circ + \alpha)$, respectively, with the horizontal direction. The ratio of their maximum heights attained is :

- (1) $\frac{1 - \tan \alpha}{1 + \tan \alpha}$
- (2) $\frac{1 + \sin \alpha}{1 - \sin \alpha}$
- (3) $\frac{1 - \sin 2\alpha}{1 + \sin 2\alpha}$
- (4) $\frac{1 + \sin 2\alpha}{1 - \sin 2\alpha}$

Ans. (3)

Sol. $H_{\text{Max}} = \frac{(u \sin \theta)^2}{2g}$

$$\frac{(H_{\text{max}})_1}{(H_{\text{max}})_2} = \frac{u^2 \sin^2 (45 - \alpha)}{u^2 \sin^2 (45 + \alpha)}$$

$$= \frac{\left(\frac{1}{\sqrt{2}} \cos \alpha - \frac{1}{\sqrt{2}} \sin \alpha\right)^2}{\left(\frac{1}{\sqrt{2}} \cos \alpha + \frac{1}{\sqrt{2}} \sin \alpha\right)^2}$$

$$= \frac{1 - \sin 2\alpha}{1 + \sin 2\alpha}$$

28. An electric dipole of mass m, charge q, and length l is placed in a uniform electric field $\vec{E} = E_0 \hat{i}$. When the dipole is rotated slightly from its equilibrium position and released, the time period of its oscillations will be :

- (1) $\frac{1}{2\pi} \sqrt{\frac{2ml}{qE_0}}$
- (2) $2\pi \sqrt{\frac{ml}{qE_0}}$
- (3) $\frac{1}{2\pi} \sqrt{\frac{ml}{2qE_0}}$
- (4) $2\pi \sqrt{\frac{ml}{2qE_0}}$

Ans. (4)

Sol. $I\omega^2 = q\ell E_0 \theta$

$$2m \left(\frac{\ell}{2}\right)^2 \omega^2 = q\ell E_0$$

$$\omega^2 = \frac{2qE_0}{m\ell}$$

$$T = 2\pi \sqrt{\frac{m\ell}{2qE_0}}$$

29. The pair of physical quantities not having same dimensions is :

- (1) Torque and energy
- (2) Surface tension and impulse
- (3) Angular momentum and Planck's constant
- (4) Pressure and Young's modulus

Ans. (2)

Sol. $[\tau] = [E]$

$$[\sigma] \neq [I]$$

$$[L] = [h]$$

$$[P] = [Y]$$

- 30.** Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

Assertion (A) : Time period of a simple pendulum is longer at the top of a mountain than that at the base of the mountain.

Reason (R) : Time period of a simple pendulum decreases with increasing value of acceleration due to gravity and vice-versa.

In the light of the above statements, choose the **most appropriate answer** from the options given below:

- (1) Both (A) and (R) are true but (R) is **not** the correct explanation of (A).
 (2) Both (A) and (R) are true and (R) is the correct explanation of (A).
 (3) (A) is true but (R) is false.
 (4) (A) is false but (R) is true.

Ans. (2)

Sol. As h increases, g decreases, T increases

$$T = 2\pi\sqrt{\frac{\ell}{g}}$$

$$g = \frac{g_0 R^2}{(R+h)^2}$$

- 31.** The expression given below shows the variation of velocity (v) with time (t), $v = At^2 + \frac{Bt}{C+t}$. The dimension of ABC is :

- (1) $[M^0 L^2 T^{-3}]$ (2) $[M^0 L^1 T^{-3}]$
 (3) $[M^0 L^1 T^{-2}]$ (4) $[M^0 L^2 T^{-2}]$

Ans. (1)

Sol. $[LT^{-1}] = [A] [T^2] = \frac{[B][T]}{[C] + [T]}$

$$[C] = [T]$$

$$[A] = [LT^{-3}]$$

$$[B] = [LT^{-1}]$$

$$[ABC] = [L^2 T^{-3}]$$

- 32.** Consider I_1 and I_2 are the currents flowing simultaneously in two nearby coils 1 & 2, respectively. If L_1 = self inductance of coil 1, M_{12} = mutual inductance of coil 1 with respect to coil 2, then the value of induced emf in coil 1 will be

$$(1) \varepsilon_1 = -L_1 \frac{dI_1}{dt} + M_{12} \frac{dI_2}{dt}$$

$$(2) \varepsilon_1 = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_1}{dt}$$

$$(3) \varepsilon_1 = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_2}{dt}$$

$$(4) \varepsilon_1 = -L_1 \frac{dI_2}{dt} - M_{12} \frac{dI_1}{dt}$$

Ans. (3)

Sol. $\phi_1 = L_1 I_1 + M_{12} I_2$

$$\varepsilon_1 = -\frac{d\phi_1}{dt} = -L_1 \frac{dI_1}{dt} - M_{12} \frac{dI_2}{dt}$$

- 33.** At the interface between two materials having refractive indices n_1 and n_2 , the critical angle for reflection of an em wave is θ_{1c} . The n_2 material is replaced by another material having refractive index n_3 , such that the critical angle at the interface between n_1 and n_3 materials is θ_{2c} . If $n_3 > n_2 > n_1$;

$$\frac{n_2}{n_3} = \frac{2}{5} \text{ and } \sin \theta_{2c} - \sin \theta_{1c} = \frac{1}{2}, \text{ then } \theta_{1c} \text{ is}$$

$$(1) \sin^{-1}\left(\frac{1}{6n_1}\right) \quad (2) \sin^{-1}\left(\frac{2}{3n_1}\right)$$

$$(3) \sin^{-1}\left(\frac{5}{6n_1}\right) \quad (4) \sin^{-1}\left(\frac{1}{3n_1}\right)$$

Ans. (4)

Sol. $\sin \theta_{1c} = \frac{n_1}{n_2}$

$$\sin \theta_{2c} = \frac{n_1}{n_3}$$

$$\sin \theta_{2c} - \sin \theta_{1c} = \frac{1}{2}$$

$$n_1 \frac{n_2}{n_3} - \frac{n_1}{n_2} = \frac{1}{2}$$

$$n_1 \frac{n_2}{n_3} - n_1 = \frac{n_2}{2}$$

$$n_1 \left(\frac{2}{5} - 1 \right) = \frac{n_2}{2}$$

$$\frac{n_1}{n_2} = \frac{-5}{6}$$

$$= \sin^{-1} \left(-\frac{5}{6} \right)$$

34. Consider a long straight wire of a circular cross-section (radius a) carrying a steady current I . The current is uniformly distributed across this cross-section. The distances from the centre of the wire's cross-section at which the magnetic field [inside the wire, outside the wire] is half of the maximum possible magnetic field, any where due to the wire, will be

- (1) $[a/4, 3a/2]$ (2) $[a/2, 2a]$
(3) $[a/2, 3a]$ (4) $[a/4, 2a]$

Ans. (2)

Sol. Maximum possible magnetic field is at the surface

$$B_{\max} = \frac{\mu_0 I}{2\pi a}$$

$$\frac{B_{\max}}{2} = \frac{\mu_0 I}{4\pi a}$$

It can be obtained inside as well as outside the wire

For inside,

$$\frac{\mu_0 I}{4\pi a} = \frac{\mu_0 I r}{2\pi a^2}$$

$$\Rightarrow r = \frac{a}{2}$$

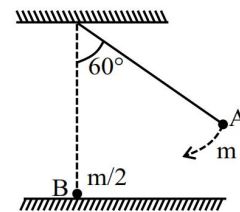
For outside

$$\frac{\mu_0 I}{4\pi a} = \frac{\mu_0 I}{2\pi r}$$

$$\Rightarrow r = 2a$$

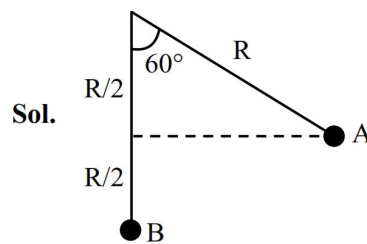
$$\text{Correct answer } \left[\frac{a}{2}, 2a \right]$$

35. As shown below, bob A of a pendulum having massless string of length 'R' is released from 60° to the vertical. It hits another bob B of half the mass that is at rest on a friction less table in the centre. Assuming elastic collision, the magnitude of the velocity of bob A after the collision will be (take g as acceleration due to gravity)



- (1) $\frac{1}{3}\sqrt{Rg}$ (2) \sqrt{Rg}
(3) $\frac{4}{3}\sqrt{Rg}$ (4) $\frac{2}{3}\sqrt{Rg}$

Ans. (1)



Sol.

Velocity of A just before hitting :

$$u = \sqrt{2g \frac{R}{2}} = \sqrt{gR}$$

Just after collision, let velocity of A and B are v_1 and v_2 respectively

\therefore by COM:

$$mu = mv_1 + \frac{m}{2}v_2$$

$$2v_1 + v_2 = 2u \quad \dots(i)$$

$$e = 1 = \frac{v_2 - v_1}{u}$$

$$\Rightarrow v_2 - v_1 = u \quad \dots(ii)$$

From (i) -(ii)

$$\Rightarrow 3v_1 = u \Rightarrow v_1 = \frac{u}{3} = \frac{1}{3}\sqrt{gR}$$

36. Given below are two statements : one is labelled as **Assertion (A)** and the other is labelled as **Reason (R)**.

Assertion (A) : Emission of electrons in photoelectric effect can be suppressed by applying a sufficiently negative electron potential to the photoemissive substance.

Reason (R) : A negative electric potential, which stops the emission of electrons from the surface of a photoemissive substance, varies linearly with frequency of incident radiation.

In the light of the above statements, choose the **most appropriate answer** from the options given below:

- (1) (A) is false but (R) is true.
 (2) (A) is true but (R) is false.
 (3) Both (A) and (R) are true and (R) is the correct explanation of (A).
 (4) Both (A) and (R) are true but (R) is **not** the correct explanation of (A).

Ans. (4)

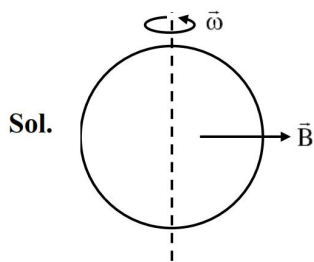
Sol. (A) : True

(B) : True but not correct explanation

37. A coil of area A and N turns is rotating with angular velocity ω in a uniform magnetic field \vec{B} about an axis perpendicular to \vec{B} . Magnetic flux ϕ and induced emf ε across it, at an instant when \vec{B} is parallel to the plane of coil, are :

- (1) $\phi = AB, \varepsilon = 0$ (2) $\phi = 0, \varepsilon = NAB\omega$
 (3) $\phi = 0, \varepsilon = 0$ (4) $\phi = AB, \varepsilon = NAB\omega$

Ans. (2)



$$\phi = BAN \cos(\omega t)$$

$$\varepsilon = \frac{-d\phi}{dt} = BA\omega N \sin(\omega t)$$

When B is parallel to plane, $\omega t = \frac{\pi}{2}$

$$\Rightarrow \phi = 0, \varepsilon = BA\omega N$$

38. The fractional compression $\left(\frac{\Delta V}{V}\right)$ of water at the depth of 2.5 km below the sea level is _____.
 Given, the Bulk modulus of water $= 2 \times 10^9 \text{ Nm}^{-2}$, density of water $= 10^3 \text{ kg m}^{-3}$, acceleration due to gravity $= g = 10 \text{ ms}^{-2}$.

- (1) 1.75 (2) 1.0
 (3) 1.5 (4) 1.25

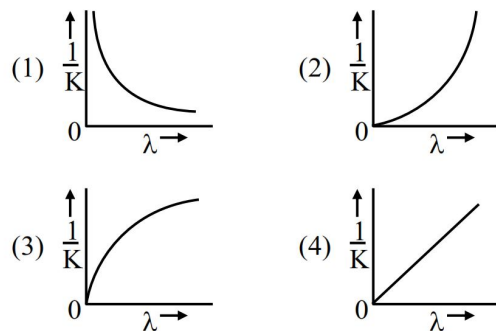
Ans. (4)

Sol. $B = \frac{\rho gh}{\left(\frac{\Delta v}{v}\right)}$

$$\frac{\Delta v}{v} \times 100 = \frac{\rho gh}{B} \times 100$$

$$\frac{1000 \times 10 \times 2.5 \times 10^3}{2 \times 10^9} \times 100\% = 1.25\%$$

39. If λ and K are de Broglie Wavelength and kinetic energy, respectively, of a particle with constant mass. The correct graphical representation for the particle will be :-



Ans. (2)

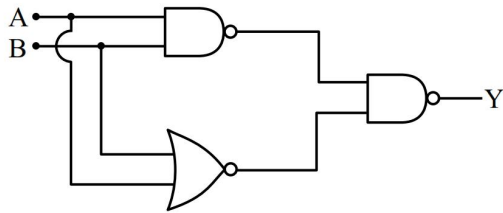
Sol. $\lambda = \frac{h}{mv} = \frac{h}{\sqrt{2mK}}$

$$\lambda^2 = \frac{h^2}{2m} \left(\frac{1}{K}\right)$$

$$Y = cx^2$$

Upward facing parabola passing through origin.

40.



For the circuit shown above, equivalent GATE is :

- (1) OR gate (2) NOT gate
(3) AND gate (4) NAND gate

Ans. (1)

A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

Sol.

⇒ OR Gate

41. A body of mass 'm' connected to a massless and unstretchable string goes in verticle circle of radius 'R' under gravity g. The other end of the string is fixed at the center of circle. If velocity at top of circular path is $n\sqrt{gR}$, where, $n \geq 1$, then ratio of kinetic energy of the body at bottom to that at top of the circle is

- (1) $\frac{n}{n+4}$ (2) $\frac{n+4}{n}$
(3) $\frac{n^2}{n^2+4}$ (4) $\frac{n^2+4}{n^2}$

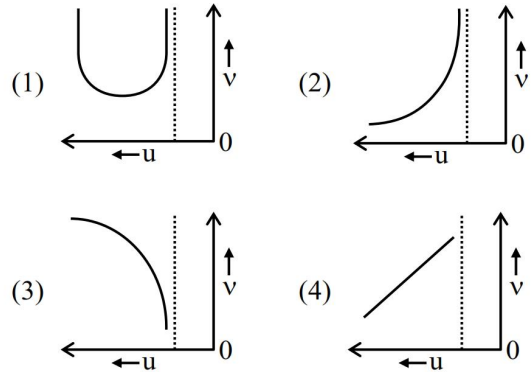
Ans. (4)

Sol. $V_{\text{Top}} = \sqrt{n^2 g R}$

$$V_{\text{Bottom}} = \sqrt{n^2 g R + 4gR}$$

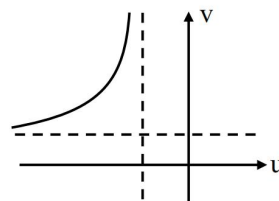
$$\text{Ratio} = \frac{n^2 + 4}{n^2}$$

42. Let u and v be the distances of the object and the image from a lens of focal length f. The correct graphical representation of u and v for a convex lens when $|u| > f$, is



Ans. (2)

Sol. $(u + f)(v - f) = f^2$



43. Match List-I with List-II.

	List-I		List-II
(A)	Electric field inside (distance $r > 0$ from center) of a uniformly charged spherical shell with surface charge density σ , and radius R.	(I)	σ / ϵ_0
(B)	Electric field at distance $r > 0$ from a uniformly charged infinite plane sheet with surface charge density σ .	(II)	$\sigma / 2\epsilon_0$
(C)	Electric field outside (distance $r > 0$ from center) of a uniformly charged spherical shell with surface charge density σ , and radius R	(III)	0
(D)	Electric field between 2 oppositely charged infinite plane parallel sheets with uniform surface charge density σ .	(IV)	$\frac{\sigma}{\epsilon_0 r^2}$

Choose the **correct** answer from the options given

below :

- (1) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)
- (2) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)
- (3) (A)-(II), (B)-(I), (C)-(IV), (D)-(III)
- (4) (A)-(III), (B)-(II), (C)-(IV), (D)-(I)

Ans. (4)

Sol. (A) \rightarrow 0 (III)

$$(B) \rightarrow \frac{\sigma}{2\epsilon_0} \text{ (II)}$$

$$(C) \rightarrow \frac{\sigma R^2}{\epsilon_0 r^2} \text{ (No row matching)}$$

$$(D) \rightarrow \frac{\sigma}{\epsilon_0} \text{ (I)}$$

44. The workdone in an adiabatic change in an ideal gas depends upon only :

- (1) change in its pressure
- (2) change in its specific heat
- (3) change in its volume
- (4) change in its temperature

Ans. (4)

Sol. $\Delta W = -\Delta U = -nC_v \Delta T$

45. Given below are two statements : one is labelled as **Assertion (A)** and other is labelled as **Reason (R)**.

Assertion (A) : Electromagnetic waves carry energy but not momentum.

Reason (R) : Mass of a photon is zero.

In the light of the above statements, choose the **most appropriate answer** from the options given below :

- (1) (A) is true but (R) is false.
- (2) (A) is false but (R) is true.
- (3) Both (A) and (R) are true but (R) is **not** the correct explanation of (A).
- (4) Both (A) and (R) are true and (R) is the correct explanation of (A).

Ans. (2)

Sol. Assertion is false because em waves have momentum.

SECTION-B

46. The coordinates of a particle with respect to origin in a given reference frame is (1, 1, 1) meters. If a force of $\vec{F} = \hat{i} - \hat{j} + \hat{k}$ acts on the particle, then the magnitude of torque (with respect to origin) in z-direction is _____.

Ans. (2)

$$\text{Sol. } \vec{\tau} = \vec{r} \times \vec{F} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 1 & 1 & 1 \\ 1 & -1 & 1 \end{vmatrix}$$

$$\vec{\tau} = \hat{k}(-1-1) = -2\hat{k}$$

$$|\vec{\tau}| = 2\text{Nm}$$

47. A container of fixed volume contains a gas at 27°C. To double the pressure of the gas, the temperature of gas should be raised to _____ °C.

Ans. (327)

$$\text{Sol. } \frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$\frac{P}{300} = \frac{2P}{T_2}$$

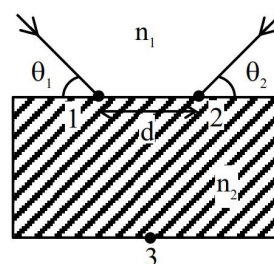
$$T_2 = 600 \text{ K}$$

$$T_2 = 327^\circ\text{C}$$

48. Two light beams fall on a transparent material block at point 1 and 2 with angle θ_1 and θ_2 , respectively, as shown in figure. After refraction, the beams intersect at point 3 which is exactly on the interface at other end of the block. Given : the distance between 1 and 2, $d = 4\sqrt{3}$ cm and

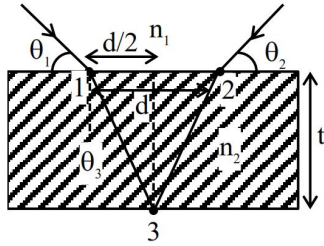
$$\theta_1 = \theta_2 = \cos^{-1}\left(\frac{n_2}{2n_1}\right), \text{ where refractive index of}$$

the block $n_2 >$ refractive index of the outside medium n_1 , then the thickness of the block is _____ cm.



Ans. (6)

Sol.



$$n_1 \sin(90 - \theta_1) = n_2 \sin \theta_3$$

$$n_1 \cos \theta_1 = n_2 \sin \theta_3$$

$$n_1 \frac{n_2}{2n_1} = n_2 \sin \theta_3$$

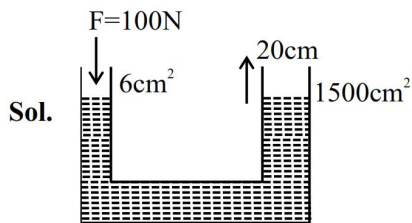
$$\frac{1}{2} = \sin \theta_3, \theta_3 = 30$$

$$\tan 30 = \frac{d}{2(t)}$$

$$t = \frac{d\sqrt{3}}{2} = \frac{4\sqrt{3} \times \sqrt{3}}{2} \text{ cm} = 6 \text{ cm}$$

49. In a hydraulic lift, the surface area of the input piston is 6 cm^2 and that of the output piston is 1500 cm^2 . If 100 N force is applied to the input piston to raise the output piston by 20 cm , then the work done is _____ kJ.

Ans. (5)



Sol.

$$\frac{F_1}{A_1} = \frac{F_2}{A_2}, \frac{100}{6} = \frac{F}{1500}, F = \frac{50}{3} \times 1500$$

$$F = 50 \times 500 = 25 \times 10^3 \text{ N}$$

$$W = \vec{F} \cdot \vec{S} = 25 \times 10^3 \times \frac{20}{100}$$

$$= 5 \times 10^3 = 5 \text{ kJ}$$

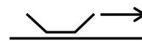
50. The maximum speed of a boat in still water is 27 km/h . Now this boat is moving downstream in a river flowing at 9 km/h . A man in the boat throws a ball vertically upwards with speed of 10 m/s . Range of the ball as observed by an observer at rest on the river bank, is _____ cm.

(Take $g = 10 \text{ m/s}^2$)

Ans. (2000)

Sol.

$$\vec{v}_b = 9 + 27 = 36 \text{ km/hr}$$



$$\vec{v}_b = 36 \times \frac{1000}{36000} = 10 \text{ m/sec}$$

$$\text{Time of flight} = \frac{2 \times 10}{10} = 2 \text{ sec}$$

$$\text{Range} = 10 \times 2 = 20 \text{ m} = 2000 \text{ cm}$$

CHEMISTRY

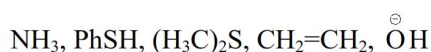
SECTION-A

51. Total number of nucleophiles from the following is :-
 NH_3 , PhSH , $(\text{H}_3\text{C})_2\text{S}$, $\text{H}_2\text{C}=\text{CH}_2$, OH^- , H_3O^+ ,
 $(\text{CH}_3)_2\text{CO}$, $\text{CH}_2=\text{NCH}_3$

- (1) 5 (2) 4
 (3) 7 (4) 6

Ans. (1)

Sol. Total five nucleophiles are present



52. The standard reduction potential values of some of the p-block ions are given below. Predict the one with the strongest oxidising capacity.

- (1) $E_{\text{Sn}^{4+}/\text{Sn}^{2+}}^\ominus = +1.15\text{V}$ (2) $E_{\text{Tl}^{3+}/\text{Tl}}^\ominus = +1.26\text{V}$
 (3) $E_{\text{Al}^{3+}/\text{Al}}^\ominus = -1.66\text{V}$ (4) $E_{\text{Pb}^{4+}/\text{Pb}^{2+}}^\ominus = +1.67\text{V}$

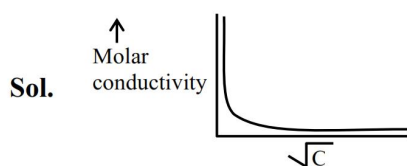
Ans. (4)

Sol. Standard reduction potential value (+ve) increases oxidising capacity increases.

53. The molar conductivity of a weak electrolyte when plotted against the square root of its concentration, which of the following is expected to be observed?

- (1) A small decrease in molar conductivity is observed at infinite dilution.
 (2) A small increase in molar conductivity is observed at infinite dilution.
 (3) Molar conductivity increases sharply with increase in concentration.
 (4) Molar conductivity decreases sharply with increase in concentration.

Ans. (4)



54. At temperature T, compound $\text{AB}_{2(\text{g})}$ dissociates as $\text{AB}_{2(\text{g})} \rightleftharpoons \text{AB}_{(\text{g})} + \frac{1}{2}\text{B}_{2(\text{g})}$ having degree of dissociation x (small compared to unity). The correct expression for x in terms of K_p and p is

- (1) $\sqrt[3]{\frac{2K_p}{p}}$ (2) $\sqrt[4]{\frac{2K_p}{p}}$
 (3) $\sqrt[3]{\frac{2K_p^2}{p}}$ (4) $\sqrt{K_p}$

Ans. (3)

Sol. $\text{AB}_{2(\text{g})} \rightleftharpoons \text{AB}_{(\text{g})} + \frac{1}{2}\text{B}_{2(\text{g})}$

$$t_{\text{eq.}} \frac{(1-x)P}{1+\frac{x}{2}} \cdot \frac{xP}{1+\frac{x}{2}} \cdot \left(\frac{x}{2}\right)^{\frac{1}{2}} \frac{P}{1+\frac{x}{2}}$$

$$\Rightarrow x \ll 1 \Rightarrow 1 + \frac{x}{2} \simeq 1 \text{ and } 1 - x \simeq 1$$

$$\Rightarrow K_p = \frac{(xP) \cdot \left(\frac{xP}{2}\right)^{\frac{1}{2}}}{P}$$

$$\Rightarrow K_p^2 = x^2 \cdot \frac{xP}{2}$$

$$x = \sqrt[3]{\frac{2K_p^2}{P}}$$

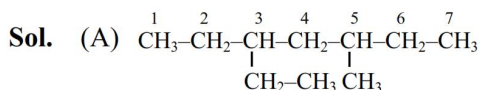
55. Match List-I with List-II.

	List-I (Structure)		List-II (IUPAC Name)
(A)	$\text{H}_3\text{C}-\text{CH}_2-\underset{\text{C}_2\text{H}_5}{\text{CH}}-\text{CH}_2-\underset{\text{CH}_3}{\text{CH}}-\text{C}_2\text{H}_5$	(I)	4-Methylpent-1-ene
(B)	$(\text{CH}_3)_2\text{C}(\text{C}_3\text{H}_7)_2$	(II)	3-Ethyl-5-methylheptane
(C)		(III)	4,4-Dimethylheptane
(D)		(IV)	2-Methyl-1,3-pentadiene

Choose the **correct** answer from the options given below:

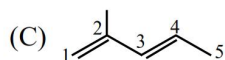
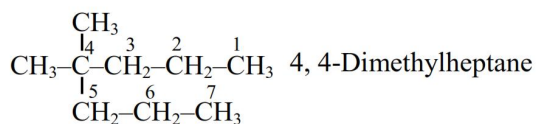
- (1) (A)-(III), (B)-(II), (C)-(IV), (D)-(I)
 (2) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
 (3) (A)-(II), (B)-(III), (C)-(IV), (D)-(I)
 (4) (A)-(II), (B)-(III), (C)-(I), (D)-(IV)

Ans. (3)

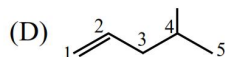


3-Ethyl-5-methylheptane

- (B) $(\text{CH}_3)_2\text{C}(\text{C}_3\text{H}_7)_2$



2-Methyl-1, 3-pentadiene



4-Methylpent-1-ene

56. Choose the **correct** statements.

- (A) Weight of a substance is the amount of matter present in it.
 (B) Mass is the force exerted by gravity on an object.
 (C) Volume is the amount of space occupied by a substance.
 (D) Temperatures below 0°C are possible in Celsius scale, but in Kelvin scale negative temperature is not possible.
 (E) Precision refers to the closeness of various measurements for the same quantity.

- (1) (B), (C) and (D) Only
 (2) (A), (B) and (C) Only
 (3) (A), (D) and (E) Only
 (4) (C), (D) and (E) Only

Ans. (4)

Sol. Theory based

57. The correct increasing order of stability of the complexes based on Δ_o value is :

- (I) $[\text{Mn}(\text{CN})_6]^{3-}$ (II) $[\text{Co}(\text{CN})_6]^{4-}$
 (III) $[\text{Fe}(\text{CN})_6]^{4-}$ (IV) $[\text{Fe}(\text{CN})_6]^{3-}$
 (1) $\text{II} < \text{III} < \text{I} < \text{IV}$ (2) $\text{IV} < \text{III} < \text{II} < \text{I}$
 (3) $\text{I} < \text{II} < \text{IV} < \text{III}$ (4) $\text{III} < \text{II} < \text{IV} < \text{I}$

Ans. (3)

- Sol.** (I) $[\text{Mn}(\text{CN})_6]^{3-}$ $-1.6 \Delta_o$
 (II) $[\text{Co}(\text{CN})_6]^{4-}$ $-1.8 \Delta_o$
 (III) $[\text{Fe}(\text{CN})_6]^{4-}$ $-2.4 \Delta_o$
 (IV) $[\text{Fe}(\text{CN})_6]^{3-}$ $-2.0 \Delta_o$
 $\text{I} < \text{II} < \text{IV} < \text{III}$

58. Match List-I with List-II.

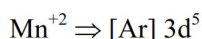
List-I (Complex)		List-II (Hybridisation & Magnetic characters)	
(A)	$[\text{MnBr}_4]^{2-}$	(I)	d^2sp^3 & diamagnetic
(B)	$[\text{FeF}_6]^{3-}$	(II)	sp^3d^2 & paramagnetic
(C)	$[\text{Co}(\text{C}_2\text{O}_4)_3]^{3-}$	(III)	sp^3 & diamagnetic
(D)	$[\text{Ni}(\text{CO})_4]$	(IV)	sp^3 & paramagnetic

Choose the **correct** answer from the options given below :

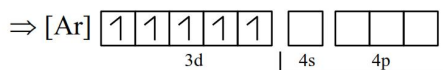
- (1) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
 (2) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)
 (3) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)
 (4) (A)-(IV), (B)-(II), (C)-(I), (D)-(III)

Ans. (4)

Sol. (A) $[\text{MnBr}_4]^{2-}$

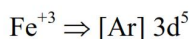


In presence of ligand field

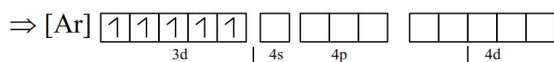


$\Rightarrow sp^3$ hybridization, paramagnetic in nature

(B) [FeF₆]

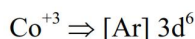


In presence of ligand field

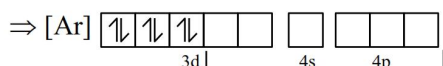


$\Rightarrow sp^3d^2$ hybridization, paramagnetic in nature

(C) [Co(C₂O₄)₃]³⁻

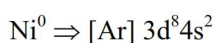


In presence of ligand field

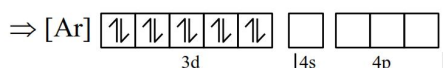


$\Rightarrow d^2sp^3$ hybridization, diamagnetic in nature

(D) [Ni(CO)₄]

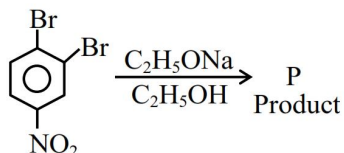


In presence of ligand field

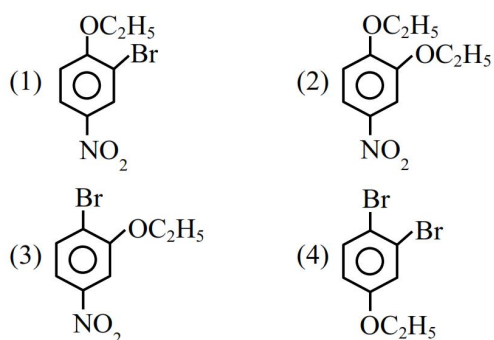


$\Rightarrow sp^3$ hybridization, diamagnetic in nature

59. In the following substitution reaction :

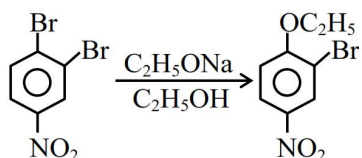


Product 'P' formed is :



Ans. (1)

Sol. It is an example of nucleophilic Aromatic substitution reaction.



60. For a $\text{Mg} | \text{Mg}^{+2}(\text{aq}) || \text{Ag}^{+}(\text{aq}) | \text{Ag}$ the correct Nernst Equation is :

$$(1) E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Ag}^{+}]}{[\text{Mg}^{2+}]}$$

$$(2) E_{\text{cell}} = E_{\text{cell}}^{\circ} + \frac{RT}{2F} \ln \frac{[\text{Ag}^{+}]^2}{[\text{Mg}^{2+}]}$$

$$(3) E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Mg}^{2+}]}{[\text{Ag}^{+}]}$$

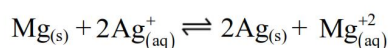
$$(4) E_{\text{cell}} = E_{\text{cell}}^{\circ} - \frac{RT}{2F} \ln \frac{[\text{Ag}^{+}]^2}{[\text{Mg}^{2+}]}$$

Ans. (2)

Sol. According to Nernst equation :-

$$E = E^{\circ} - \frac{RT}{nF} \ln Q.$$

Cell reaction :-



$$\Rightarrow Q = \frac{[\text{Mg}^{+2}]}{[\text{Ag}^{+}]^2}$$

$$\Rightarrow E = E_{\text{Cell}}^{\circ} - \frac{RT}{2F} \ln \left[\frac{[\text{Mg}^{+2}]}{[\text{Ag}^{+}]^2} \right]$$

61. The correct option with order of melting points of the pairs (Mn, Fe), (Tc, Ru) and (Re, Os) is :

- (1) $\text{Fe} < \text{Mn}$, $\text{Ru} < \text{Tc}$ and $\text{Re} < \text{Os}$
- (2) $\text{Mn} < \text{Fe}$, $\text{Tc} < \text{Ru}$ and $\text{Re} < \text{Os}$
- (3) $\text{Mn} < \text{Fe}$, $\text{Tc} < \text{Ru}$ and $\text{Os} < \text{Re}$
- (4) $\text{Fe} < \text{Mn}$, $\text{Ru} < \text{Tc}$ and $\text{Os} < \text{Re}$

Ans. (3)

Sol. M.P. $\Rightarrow \text{Mn} < \text{Fe}$, $\text{Tc} < \text{Ru}$, $\text{Os} < \text{Re}$

NCERT based

62. 1.24 g of AX_2 (molar mass 124 g mol⁻¹) is dissolved in 1 kg of water to form a solution with boiling point of 100.0156°C, while 25.4 g of AY_2 (molar mass 250 g mol⁻¹) in 2 kg of water constitutes a solution with a boiling point of 100.0260°C.

$$K_b(\text{H}_2\text{O}) = 0.52 \text{ K kg mol}^{-1}$$

Which of the following is correct ?

- (1) AX_2 and AY_2 (both) are completely unionised.
- (2) AX_2 and AY_2 (both) are fully ionised.
- (3) AX_2 is completely unionised while AY_2 is fully ionised.
- (4) AX_2 is fully ionised while AY_2 is completely unionised.

Ans. (4)

Sol. For AX_2 :- $\Delta T_b = K_b \times m \times i$

$$0.0156 = 0.52 \times \frac{0.01}{1} \times i_{AX_2}$$

$$\Rightarrow i_{AX_2} = 3 \Rightarrow \text{complete ionisation}$$

For AY_2 :- $\Delta T_b = K_b \times m \times i$

$$0.026 = 0.52 \times 0.0508 \times i_{AY_2}$$

$$\Rightarrow i_{AY_2} \simeq 1 \therefore \text{complete unionisation}$$

- 63.** 500 J of energy is transferred as heat to 0.5 mol of Argon gas at 298 K and 1.00 atm. The final temperature and the change in internal energy respectively are :

Given : $R = 8.3 \text{ J K}^{-1} \text{ mol}^{-1}$

- (1) 348 K and 300 J
- (2) 378 K and 300 J
- (3) 368 K and 500 J
- (4) 378 K and 500 J

Ans. (4)

Sol. $q_p = n \times c_p \times \Delta T$

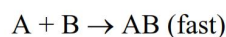
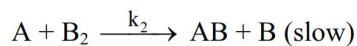
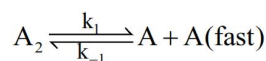
$$\Rightarrow 500 = 0.5 \times \frac{5}{2} \times 8.3 (T_f - 298)$$

$$\Rightarrow T_f \simeq 346.2 \text{ K}$$

$$\frac{\Delta H}{\Delta U} = \frac{C_p}{C_v} = \left(\frac{5}{3} \right)$$

$$\Rightarrow \Delta U = \frac{3}{5} \times 500 = 300 \text{ J}$$

- 64.** The reaction $A_2 + B_2 \rightarrow 2 AB$ follows the mechanism



The overall order of the reaction is :

- (1) 1.5
- (2) 3
- (3) 2.5
- (4) 2

Ans. (1)

Sol. rate = $k_2[A][B_2]$ (1)

$$\left(\frac{k_1}{k_{-1}} \right) = \left(\frac{[A]^2}{[A_2]} \right)$$

$$\Rightarrow [A] = \sqrt{\frac{k_1}{k_{-1}}} \cdot \sqrt{[A_2]}$$

Substituting in (1) ; we get

$$\text{Rate} = k_2 \sqrt{\frac{k_1}{k_{-1}}} \cdot [A_2]^{\frac{1}{2}} \cdot [B_2]$$

$$\therefore \text{order} = \left(\frac{3}{2} \right) = 1.5$$

- 65.** If a_0 is denoted as the Bohr radius of hydrogen atom, then what is the de-Broglie wavelength (λ) of the electron present in the second orbit of hydrogen atom ? [n : any integer]

- (1) $\frac{2a_0}{n\pi}$
- (2) $\frac{8\pi a_0}{n}$
- (3) $\frac{4\pi a_0}{n}$
- (4) $\frac{4n}{\pi a_0}$

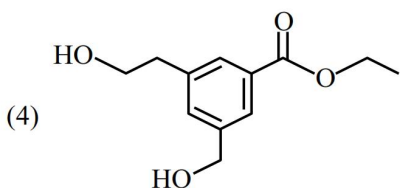
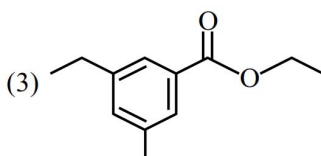
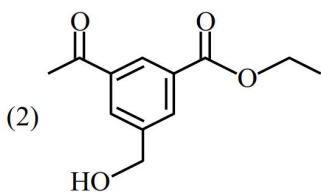
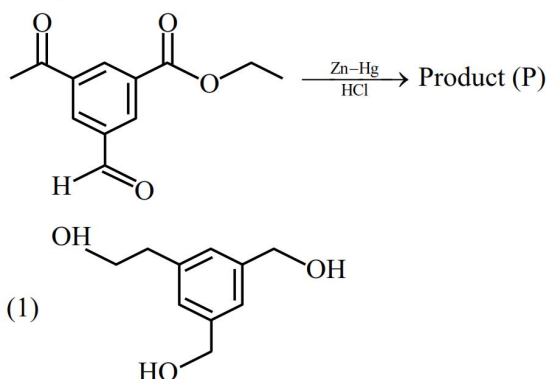
Ans. (2)

Sol. $2\pi r_n = n\lambda$

$$2\pi (4a_0) = n\lambda$$

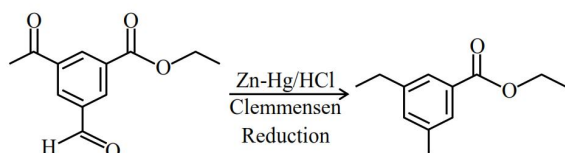
$$= \lambda = \frac{8\pi a_0}{n}$$

66. The product (P) formed in the following reaction is :



Ans. (3)

Sol.



67. An element 'E' has the ionisation enthalpy value of 374 kJ mol^{-1} . 'E' reacts with elements A, B, C and D with electron gain enthalpy values of -328 , -349 , -325 and -295 kJ mol^{-1} , respectively.

The correct order of the products EA, EB, EC and ED in terms of ionic character is :

- (1) $\text{EB} > \text{EA} > \text{EC} > \text{ED}$
- (2) $\text{ED} > \text{EC} > \text{EA} > \text{EB}$
- (3) $\text{EA} > \text{EB} > \text{EC} > \text{ED}$
- (4) $\text{ED} > \text{EC} > \text{EB} > \text{EA}$

Ans. (1)

Sol. Difference between I.E. & E.G.E increases, ionic character increases.

68. Match List – I with List – II.

List – I
(Carbohydrate)

List – II
(Linkage Source)

- | | |
|-----------------|---|
| (A) Amylose | (I) $\beta\text{-C}_1\text{-C}_4$, plant |
| (B) Cellulose | (II) $\alpha\text{-C}_1\text{-C}_4$, animal |
| (C) Glycogen | (III) $\alpha\text{-C}_1\text{-C}_4$, $\alpha\text{-C}_1\text{-C}_6$, plant |
| (D) Amylopectin | (IV) $\alpha\text{-C}_1\text{-C}_4$, plant |

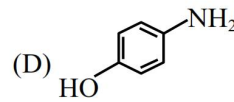
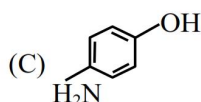
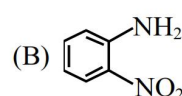
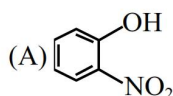
Choose the **correct** answer form the options given below :

- (1) (A)-(III), (B)-(II), (C)-(I), (D)-(IV)
- (2) (A)-(IV), (B)-(I), (C)-(II), (D)-(III)
- (3) (A)-(II), (B)-(III), (C)-(I), (D)-(IV)
- (4) (A)-(IV), (B)-(I), (C)-(III), (D)-(II)

Ans. (2)

Sol. Informative

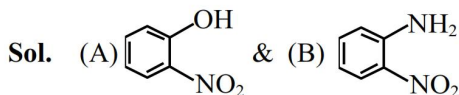
69. The steam volatile compounds among the following are :



Choose the **correct** answer from the options given below :

- (1) (B) and (D) only
- (2) (A) and (C) only
- (3) (A) and (B) only
- (4) (A),(B) and (C) only

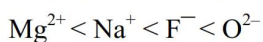
Ans. (3)



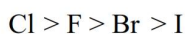
are steam volatile due to intramolecular hydrogen bonding.

70. Given below are two statements :

Statement (I) : The radii of isoelectronic species increases in the order.



Statement (II) : The magnitude of electron gain enthalpy of halogen decreases in the order.



In the light of the above statements, choose the **most appropriate answer** from the options given below :

- (1) **Statement I** is incorrect but **Statement II** is correct
- (2) Both **Statement I** and **Statement II** are incorrect
- (3) **Statement I** is correct but **Statement II** is incorrect
- (4) Both **Statement I** and **Statement II** are correct

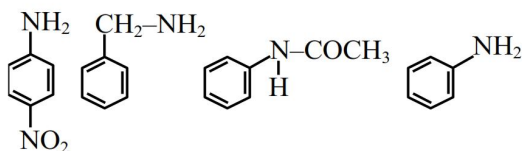
Ans. (4)

Sol. (i) For isoelectronic species -ve charge increases, radii increases.

(ii) Magnitude of E.G.E : $\text{Cl} > \text{F} > \text{Br} > \text{I}$

SECTION-B

71. Given below are some nitrogen containing compounds.

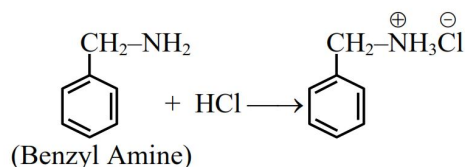


Each of them is treated with HCl separately. 1.0 g of the most basic compound will consume _____ mg of HCl.

(Given molar mass in g mol^{-1} C:12, H : 1, O : 16, Cl : 35.5)

Ans. (341)

Sol. Benzyl Amine is most basic due to localised lone pair.



$$\text{Mole of benzyl Amine} \Rightarrow \frac{1}{107} = 0.00934 \text{ mole}$$

1 Mole of Benzyl amine consumed 1 mole of HCl

So, Mole of HCl consumed $\rightarrow 0.00934$ mole

Mass of HCl consumed $\rightarrow 0.00934 \times \text{molar mass of HCl}$

$$= 0.00934 \times 36.5$$

$$= 0.341 \text{ gm}$$

$$= 341 \text{ mg}$$

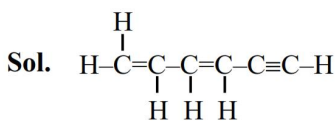
72. The molar mass of the water insoluble product formed from the fusion of chromite ore (FeCr_2O_4) with Na_2CO_3 in presence of O_2 is _____ g mol^{-1} .

Ans. (160)

Sol. $4\text{FeCr}_2\text{O}_4 + 8\text{Na}_2\text{CO}_3 + 7\text{O}_2 \rightarrow 8\text{Na}_2\text{CrO}_4 + 2\text{Fe}_2\text{O}_3 + 8\text{CO}_2$
 Fe_2O_3 is water insoluble, so its molar mass
 $\Rightarrow [2 \times 56 + 3 \times 16] \Rightarrow 160 \text{ g/mol}$

73. The sum of sigma (σ) and pi (π) bonds in Hex-1,3-dien-5-yne is _____.

Ans. (15)



Number of σ bond = 11

Number of π bond = 4

$$\sigma + \pi = 11 + 4 = 15$$

74. If A_2B is 30% ionised in an aqueous solution, then the value of van't Hoff factor (i) is _____ $\times 10^{-1}$.

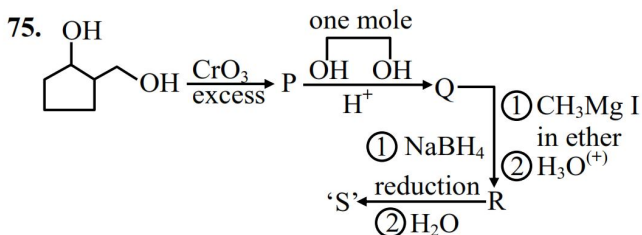
Ans. (16)

Sol. $\text{A}_2\text{B} \rightarrow 2\text{A}^+ + \text{B}^{2-}$; $y = 3$

$$\alpha = 0.3$$

$$i = 1 + (y - 1)\alpha$$

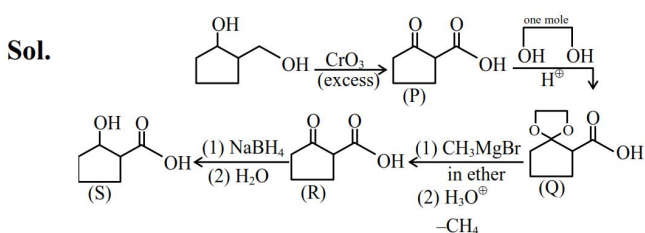
$$= 1 + (3 - 1)(0.3) = 1.6 = 16 \times 10^{-1}$$



0.1 mole of compound 'S' will weigh _____ g.

(Given molar mass in g mol^{-1} C:12, H:1, O:16)

Ans. (13)



0.1 mole of compound (S) weight in gm

$$= 0.1 \times \text{molar mass of compound (S)}$$

$$= 0.1 \times 130 = 13 \text{ gm}$$